

Ideal Gas Law

$$PV = nRT$$

Re-arrange the constants

$$PV = nRT$$

$$PV = nN_a \left(\frac{R}{N_a} \right) T$$

Ideal Gas Law expressed with Boltzmann's Constant

$$PV = nRT$$

$$PV = nN_a \left(\frac{R}{N_a} \right) T$$

$$PV = NkT$$

Ideal Gas Law

$$PV = nRT = NkT$$

Force During a Elastic Molecular Collision

$$F = ma$$

Force During a Elastic Molecular Collision

$$\begin{aligned} F &= ma \\ &= m \frac{\Delta v}{\Delta t} \end{aligned}$$

Force During a Elastic Molecular Collision

$$\begin{aligned} F &= ma \\ &= m \frac{\Delta v}{\Delta t} \\ &= \frac{\Delta(mv)}{t} \end{aligned}$$

Force on the molecule per collision

$$F = \frac{\Delta(mv)}{t}$$

Force on the molecule per collision

$$F = \frac{\Delta(mv)}{t}$$
$$\frac{-mv - (mv)}{2L / v}$$

Force on the molecule per collision

$$\begin{aligned} F &= \frac{\Delta(mv)}{t} \\ &= \frac{-mv - (mv)}{2L / v} \\ &= \frac{-2mv^2}{2L} \end{aligned}$$

Force on the molecule per collision

$$\begin{aligned} F &= \frac{\Delta(mv)}{t} \\ &= \frac{-mv - (mv)}{2L / v} \\ &= \frac{-2mv^2}{2L} \\ &= \frac{-mv^2}{L} \end{aligned}$$

Force on the side of a cube per molecular collision

$$F = \frac{mv^2}{L}$$

Total force on a side of a cube

$$F = \frac{mv^2}{L}$$
$$= \left(\frac{N}{3} \right) \left(\frac{\overline{mv^2}}{L} \right)$$

Total force on a side of a cube

$$\begin{aligned} F &= \frac{mv^2}{L} \\ &= \left(\frac{N}{3} \right) \left(\frac{\overline{mv^2}}{L} \right) \\ &= \frac{N}{3L} (mv_{rms}^2) \end{aligned}$$

Converting Force into Pressure

$$P = \frac{F}{A}$$

Pressure on a side of the cube

$$P = \frac{F}{A}$$
$$= \frac{F}{L^2}$$

Pressure on side of the cube

$$\begin{aligned} P &= \frac{F}{A} \\ &= \frac{F}{L^2} \\ &= \frac{N}{3L} \frac{(mv_{rms}^2)}{L^2} \end{aligned}$$

Pressure on side of the cube

$$\begin{aligned} P &= \frac{F}{A} \\ &= \frac{F}{L^2} \\ &= \frac{\frac{N}{3L} (mv_{rms}^2)}{L^2} \\ &= \frac{N}{3L^3} (mv_{rms}^2) \end{aligned}$$

Pressure on side of the cube

$$\begin{aligned} P &= \frac{F}{A} \\ &= \frac{F}{L^2} \\ &= \frac{N}{3L^3} (mv_{rms}^2) \\ &= \frac{N}{3V} (mv_{rms}^2) \end{aligned}$$

Pressure on side of the cube

$$P = \frac{N}{3V} (mv_{rms}^2)$$

Pressure on side of the cube

$$P = \frac{N}{3V} (mv_{rms}^2)$$

$$PV = \frac{N}{3} (mv_{rms}^2)$$

Pressure on side of the cube

$$P = \frac{N}{3V} (mv_{rms}^2)$$

$$PV = \frac{N}{3} (mv_{rms}^2)$$

$$PV = \frac{2N}{3} \left(\frac{mv_{rms}^2}{2} \right)$$

Pressure x Volume

$$P = \frac{N}{3V} (mv_{rms}^2)$$

$$PV = \frac{N}{3} (mv_{rms}^2)$$

$$PV = \frac{2N}{3} \left(\frac{mv_{rms}^2}{2} \right)$$

$$PV = \frac{2N}{3} (\overline{KE})$$

Pressure on each side of the cube

$$P = \frac{N}{3V} (mv_{rms}^2)$$

$$PV = \frac{N}{3} (mv_{rms}^2)$$

$$PV = \frac{2N}{3} \left(\frac{mv_{rms}^2}{2} \right)$$

$$PV = \frac{2}{3} N \left(\frac{3}{2} kT \right) = \frac{2}{3} N (\overline{KE})$$

$$\frac{3}{2} kT = \overline{KE} = \frac{1}{2} mv_{rms}^2$$

Conclusion

$$\overline{(KE)} = \frac{3}{2} kT$$

$$\frac{mv_{rms}^2}{2} = \frac{3}{2} kT$$

Related Links

- <http://www.zappinternet.com/video/fiqXvoBloZ/Kinetic-Theory-Of-Gases>